

**MAPL699, Applied Mathematics Seminar**  
**Spring 2001, Optimization and Equilibrium Problems**  
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